

## Master 2.15a

## Unit Test: Unit 2 Powers and Exponent Laws

1. Complete this table.

Power	Base	Exponent	Repeated Multiplication	Standard Form
$3^5$				
$(-2)^4$				
	10	3		
			$-(2 \times 2 \times 2 \times 2 \times 2 \times 2)$	

2. Write as a power of 10.

a) ten \_\_\_\_\_

b)  $10 \times 10 \times 10 \times 10$  \_\_\_\_\_

c)  $-1$  \_\_\_\_\_

d) 10 000 000 \_\_\_\_\_

3. Write each expression as a product or quotient of powers.

a)  $(2 \times 3)^5$  \_\_\_\_\_

b)  $\left(\frac{1}{3}\right)^2$  \_\_\_\_\_

c)  $(12 \div 4)^3$  \_\_\_\_\_

4. Write each power of a power as a single power, then evaluate it.

a)  $(9^8)^0$  \_\_\_\_\_

b)  $[(-2)^4]^2$  \_\_\_\_\_

c)  $-(3^2)^3$  \_\_\_\_\_

5. Write each expression as a power, then evaluate it.

a)  $3^3 \times 3^2$

b)  $(-2)^4 \times (-2)^0$

c)  $5^{11} \div 5^{10}$

d)  $10^8 \times 10^2 \div 10^6$

e)  $\frac{(-3)^5 \times (-3)^6}{(-3)^7 \times (-3)^1}$

## Master 2.15b

## Unit Test continued

6. a) For each pair of powers, which power is greater?

i)  $8^3$  or  $3^8$  \_\_\_\_\_      ii)  $2^{10}$  or  $10^2$  \_\_\_\_\_      iii)  $5^1$  or  $1^5$  \_\_\_\_\_

b) How could you answer part a without calculating the value of both powers?

---

---

7. a) Evaluate each power.

i)  $-2^4$  \_\_\_\_\_      ii)  $(-2^4)$  \_\_\_\_\_      iii)  $(-2)^4$  \_\_\_\_\_

b) Explain why all the powers in part a do not have the same value.

---

---

8. Evaluate each expression. Show your work.

a)  $(-14 - 6)^2 + 11$

b)  $8 \div (-2) + (4 \times 2)^2$

c)  $[7 - (-3)]^4 - (30 \div 6)^4$

d)  $[(4 - 10)^3 \times (3 + 3)^5]^0$

e)  $(6 - 8)^5 \div (-4)$

f)  $-40 - (8 - 3)^3$

g)  $2^4 \times 2^1 - 2^3 \times 2^2$

h)  $4^2 \times 4 + 3^3 \times 3^2$

i)  $(-4)^3 \div (-4)^2 \times (-4)^0 + (-4)^2 \div (-4)$

## Master 2.15c

## Unit Test continued

9. Insert brackets to make this equation correct.

$$5 \times 4^2 - 2^3 + 3^3 \div 3 = 49$$

10. Both Hayley and Gavin evaluated this expression:  $(-3^4 \times 4 - 1) \div (-5)^2$   
 Hayley's answer was 13 and Gavin's answer was -13.  
 Who is correct?  
 What is the likely error the other student made?

11. One square metre measures 1 m by 1 m.

- a) Write  $1 \text{ m}^2$  in square centimetres as a product of powers and as a single power.

\_\_\_\_\_

- b) Write  $1 \text{ m}^2$  in square millimetres as a product of powers and as a single power.

\_\_\_\_\_

12. Simplify, then evaluate each expression. Show your work.

a)  $[(-3)^3]^3 \times [(-4)^0]^3 - [(-3)^5]^0$

b)  $[(-4) \times (-5)]^4 + [(-4)^2]^2 - [(-2)^8 \div (-2)^7]^3$

13. On a test, Randy used his calculator to evaluate this expression:  $\frac{9^4}{9^2 + (-9)^2}$

The answer that was displayed was 162.

- a) Is this answer correct? \_\_\_\_\_

- b) If your answer is no, what error did Randy make? \_\_\_\_\_

- c) Show the solution to the problem to verify your answer in part a.

**Master 2.16a**

**Unit 2 Test Sample Answers**

1.

Power	Base	Exponent	Repeated Multiplication	Standard Form
$3^5$	3	5	$3 \times 3 \times 3 \times 3 \times 3$	243
$(-2)^4$	-2	4	$(-2)(-2)(-2)(-2)$	16
$10^3$	10	3	$10 \times 10 \times 10$	1000
$-(2^6)$	2	6	$-(2 \times 2 \times 2 \times 2 \times 2 \times 2)$	-64

2. a)  $10^1$       b)  $10^4$   
 c)  $-10^0$       d)  $10^7$
3. a)  $2^5 \times 3^5$     b)  $\frac{1^2}{3^2}$   
 c)  $12^3 \div 4^3$
4. a)  $9^0 = 1$       b)  $(-2)^8 = 256$   
 c)  $-(3^6) = -729$
5. a)  $3^5 = 243$     b)  $(-2)^4 = 16$   
 c)  $5^1 = 5$       d)  $10^4 = 10\,000$   
 e)  $(-3)^3 = -27$
6. a) i)  $3^8$  is greater.  
 b) i)  $8^3 = 8 \times 8 \times 8$   
 $3^8 = (3 \times 3) \times (3 \times 3) \times (3 \times 3) \times (3 \times 3)$   
 $= 9 \times 9 \times 9 \times 9 = 9^4$   
 Both the base and exponent of  $9^4$  are greater than those of  $8^3$ .  
 a) ii)  $2^{10}$  is greater.  
 b) ii)  $10^2 = 100$   
 $2^{10} = 2^3 \times 2^3 \times 2^3 \times 2 = 8 \times 8 \times 8 \times 2$ ;  
 since  $8 \times 8 = 64$ , then  $8 \times 8 \times 8$  is much greater than 100.  
 a) iii)  $5^1$  is greater.  
 b) iii) When a power has a base 1, its value is always 1, so  $5^1$  is greater than  $1^5$ .

7. a), b) i)  $-2^4 = -2 \times 2 \times 2 \times 2 = -16$ ; the base is 2, so  $2^4$  is 16; the power is negative, so  $-2^4 = -16$   
 ii)  $(-2^4)$ ; this is the same expression as in part a, but without the brackets. The brackets are not needed. So,  $(-2^4) = -16$   
 iii)  $(-2)^4 = (-2) \times (-2) \times (-2) \times (-2) = 16$ ; the base is -2 and an even number of negative factors gives a positive product.

8. a) 411      b) 60  
 c) 9375      d) 1  
 e) 8          f) -165  
 g) 0          h) 307  
 i) -8
9.  $5 \times (4^2 - 2^3) + 3^3 + 3$
10. Gavin is correct. Here is the correct solution.  
 $(-3^4 \times 4 - 1) \div (-5)^2 = (-81 \times 4 - 1) \div (-5)^2 = (-324 - 1) \div 25 = (-325) \div 25 = -13$   
 Hayley might have included the negative sign in the second power.  
 Here is Hayley's possible solution.  
 $(-34 \times 4 - 1) \div (-5)2 = (-81 \times 4 - 1) \div (-5)^2 = (-324 - 1) \div (-25) = (-325) \div (-25) = 13$
11. a)  $1 \text{ m}^2 = 10^2 \text{ cm} \times 10^2 \text{ cm} = 10^4 \text{ cm}^2$   
 b)  $1 \text{ m}^2 = 10^3 \text{ mm} \times 10^3 \text{ mm} = 10^6 \text{ mm}^2$
12. a) -19 684    b) 160 264
13. a) No  
 b) Randy forgot to insert brackets around the expression in the divisor.  
 c)  $\frac{9^4}{9^2 + (-9)^2} = \frac{9^4}{(9^2 + (-9)^2)}$   
 He could key in:  
 $9 \wedge 4 \div (9 \wedge 2 + ((-9) \wedge 2))$  to get 40.5